

Cover Image Color montage of morning overpass AMSR2 horizontally-polarized 36 GHz passive microwave brightness temperatures, 29–30 June, 2003.
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1 Revision History

Table 1: ATBD Revision History

Revision	Date	Purpose
1.0	2024-05-14	Initial Version

 Table 2: Data Set Revision History

Revision Date		Purpose				
1.0	2024-05-14	Initial Data Release				

2 Acronyms and Abbreviations

 Table 3: List of Acronyms and Abbreviations

Seasat	Advanced Earth Observing Satellite
ATBD	Algorithm Theoretical Basis Document
AVE	weighted AVEraging image formation algorithm
bSIR	Scatterometer Image Reconstruction using binary response function
BYU	Brigham Young University
CDR	Climate Data Record
CETB	Calibrated Passive Microwave Daily EASE-Grid 2.0 Brightness Temperature
CF	Climate and Forecast Metadata Conventions
DAAC	Distributed Active Archive Center
dB	decibel $(10\log_{10})$
DDP	Digitial Doppler Processor
DIB	Drop-In-the-Bucket averaging (used to produce GRD products)
doy	day of the year
E2N	EASE-Grid 2.0, Northern Hemisphere Projection
E2S	EASE-Grid 2.0, Southern Hemisphere Projection
E2T	EASE-Grid 2.0, Temperate and Tropical Cylindrical Projection
EASE-Grid	Equal-Area Scalable Earth Grid (Original Definition)
EASE-Grid 2.0	Equal-Area Scalable Earth Grid Version 2.0
EASE2-M	EASE-Grid 2.0, Mid- and Low-Latitude Cylindrical Projection
EASE2-N	EASE-Grid 2.0, Northern Hemisphere Projection
EASE2-S	EASE-Grid 2.0, Southern Hemisphere Projection
EASE2-T	EASE-Grid 2.0, Temperate and Tropical Cylindrical Projection
EIA	Earth Incidence Angle
EOSDIS	Earth Observing System Data and Information System
ESDR	Earth System Data Record
FA	incidence-angle Fixed Azimuth modulation coefficients
FCDR	Fundamental Climate Data Record
GHz	GigaHertz
GRD	(Drop-In-the-Bucket) Gridding Method
HH	Horizontal-polarization transmit, Horizontal-polarization receive
ltod	local-time-of-day
MEaSUREs	Making Earth System Data Records for Use in Research Environments
MHz	MegaHertz
MRF	Measurement Response Function
NASA	National Aeronautics and Space Administration

Acronyms and Abbreviations

SASS NASA Scatterometer

NOAA National Oceanic and Atmospheric Administration NORAD North American Aerospace Defense Command

NSIDC National Snow and Ice Data Center NetCDF Network Common Data Format

PODAAC Physical Oceanography Distributed Active Archive Center

PRF Pulse Repetition Frequency
PSRF Pixel Spatial Response Function

rSIR radiometer version of SIR SAR Synthetic Aperture Radar SASS Seasat Scatterometer

SCP Scatterometer Climate Record Pathfinder

SDR Sensor Data Record

Sigma-0 normalized radar cross section or backscatter (σ^o)

SIR Scatterometer Image Reconstruction

TBD To Be Determined TLE Two-Line Element

UTC Coordinated Universal Time

VA incidence-angle Variable Azimuth modulation coefficients
VV Vertical-polarization transmit, Vertical-polarization receive

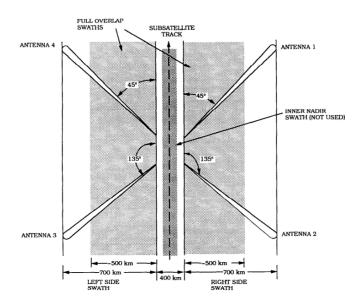


Figure 1: SASS observation swath. Nominally 50 km σ^o measurements are collected over two swaths separated by a nadir gap. Measurements are not collected over the central (nadir) gap (Grantham et al., 1977).

3 Purpose of this Document

This documents describes the CETB-compatible radar backscatter product "SASS Scatterometer Twice-Daily SIR-Enhanced EASE-Grid 2.0 Radar Backscatter", (NSIDC-0787, doi:10.5067/46IY834H created from 14.6 GHz Seasat Scatterometer (SASS) observations collected during the Seasat mission in 1979.

SASS collected nominally 50 km resolution normalized radar cross section (σ^o) from 4 different azimuth angles over two \sim 500 km wide swaths with. All four antennas were dual-polarized, resulting in 8 'beams'. SASS employed long, fan-beam antennas with narrow (\sim 10 km) narrow beamwidths, see Fig. 1. Along-beam resolution was achieved using 4.8 ms continuous wave (CW) transmit pulses and multiple analog bandpass filters to achieve along-beam resolution via band pass filtering of the echo (Grantham et al., 1977). The multiple beams provided azimuth diversity of the σ^o measurements, which is required to retrieve the surface wind (Ulaby and Long, 2014, Naderi et al., 1991, Boggs, 1981, Johnson et al., 1980).

While designed and optimized for ocean observation, SASS also collected σ^o measurements over land and ice. The observed σ^o depends on the surface roughness, geometry, and dielectric constant. These depend on geophysical parameters of interest such as surface freeze/thaw state, snow and ice structure, moisture content, and vegetation characteristics, among others (Ulaby and Long, 2014). The SASS data set provides a unique "snapshot" of

the Earth during its mission lifetime.

This CETB backscatter product exploits the SASS measurements to create a unique backscatter image data set that captures the state of the Earth during the SASS mission (1978). To exploit this data, we employ image reconstruction techniques to create daily and twicedaily enhanced resolution SASS radar images from the measurements. The new data set is provided to the science community to support cryosphere and climate studies.

4 Gridded and SIR-Enhanced SASS Product Description

4.1 Product Description

The SASS radar backscatter (*SASS*) product includes Level 1 gridded, twice-daily, radar backscatter data collected at 14.6 GHz for two radar channels (horizontal transmit-horizontal receive [HH] and vertical transmit-vertical receive [VV]. Data are gridded to the EASE-Grid 2.0 Azimuthal and Cylindrical projections (Brodzik et al., 2012, 2014), at two spatial resolutions, as described below. The *SASS* product is archived and distributed by the NSIDC DAAC (https://nsidc.org/data/NSIDC-0787/versions/1).

Input data for the *SASS* v1.0 product are the SASS Sensor Data Records (SDR) file (Boggs, 1981). They were obtained in the mid 1980's from the Jet Propulsion Laboratory Physical Oceanography Distributed Active Archive Center (PODAAC) on 9 track tapes, along with Fortran read software that included a list of bad files. The individual files on the tapes were transferred to CD-ROMS in the early 1990's by students at Brigham Young University. The reader software was translated to C with new routines to compute the binary and full response MRFs. When producing the *SASS* product the quality flags in the input data were used to select only the highest quality measurements to be included in *SASS* product. The data coverage is global (with the exception of an area immeditately around the poles) for the period beginning 7 July 1978 (doy 188) through 10 Oct 1978 (doy 283). No calibration corrections (Birrer et al., 1982, Long and Skouson, 1995) have been applied to the reported SASS σ^o measurements.

4.2 SASS Instrument

SASS flew as an attached payload on the Seasat spacecraft, which was launched on 27 June 1978 and operated for approximately $\sim\!108$ days before the spacecraft power system failed. Seasat flew in a sun-synchronous 800 km circular polar orbit with an orbit inclination angle of 108° . The SASS instrument is described in Grantham et al. (1977). SASS is a fanbeam Doppler scatterometer (Ulaby and Long, 2014) that employed fixed analog filters for obtaining along-beam resolution.

The SASS instrument employed four 3 m long fan-beam antennas deployed to provide two azimuth angle observations on each side of the spacecraft. The antennas operated in dual polarization (HH and VV), see Fig. 1. Along-track resolution was provided by the narrow beamwidth of the antenna beams and the pulse timing. Along-beam resolution was provided via Doppler filtering, see Fig. 2.

The return echo was Doppler filtered using the DDP into 15 measurement "cells", three of which were designated "monitor cells" within the inner swath. The SASS swath and measurement geometry (Fig. 2) produced a 4-sided instantaneous 3-dB footprint for each pulse. A total of 25 sequential pulses were issued for each of the 8 beams in sequence during

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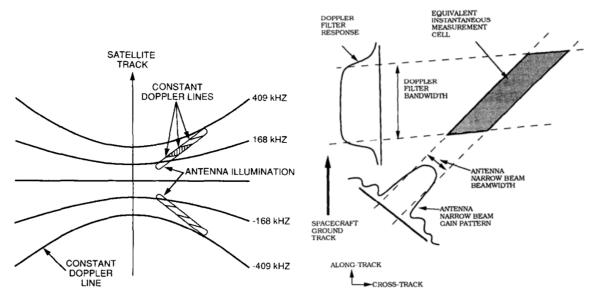


Figure 2: SASS measurement theory illustrations. (left) Intersection of the fan-beam footprint and iso-Doppler lines used to define the along-beam resolution. (right) Antenna pattern and Doppler filtering that define the individual σ^o measurement footprints for a forward-facing antenna.

the time it takes for the spacecraft to travel 50 km resulting in an along-track spacing of 50 km between along-track measurements from the same azimuth angle (Boggs, 1981).

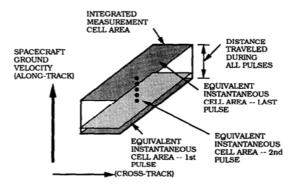


Figure 3: Illustration of the footprint when integrating multiple pulses into a single measurement (Long et al., 1993).

The 25 pulses were processed and summed into a single measurement. As shown in Fig. 3,t his produces six-sided 3-dB footprints on the surface (Boggs, 1981, Grantham et al., 1977). Assigning 1 to areas within the 3-dB footprint and 0 outside results in a simplified *binary* description of the measurement's MRF. The *full response* includes the filter and antenna pattern rolloff. An example of the layout of the binary footprints is shown in Fig. 4, The

full response minimizes coverage gaps, but is slightly smoother than the binary response when used in SIR or AVE. Examples of the full response for several SASS measurements are illustrated in Fig. 5. Image examples based on the binary response are shown in Section 6. Further comparisons of the full and binary responses are provided in Section 6.3.

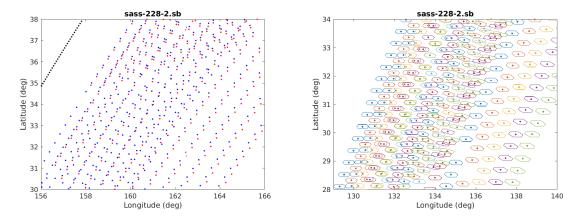


Figure 4: SASS footprint examples. (left) Measurement centers shown in color. Spacecraft nadir shown in black dots. (right) 3-dB integrated footprint outline illustrating the binary response approximation.

Note that while a radiometer's footprint is defined by the antenna pattern, the radar footprint is defined by the antenna pattern squared due to the two-way travel of the signal from radar to the surface (Ulaby and Long, 2014).

SASS collected return echo power measurements, which were converted into σ^o using the radar equation (JPL, 1997, Ulaby and Long, 2014). The nominal resolution of these measurements is described as 25 km, though the effective resolution varies over the swath and orbit. The σ^o value depends on the surface roughness, geometry, and dielectric constant (Ulaby and Long, 2014).

To better understand the spatial layout of the SASS σ^o measurements Figure 6 shows the positions of the centers of all the σ^o measurements from a single orbit pass. Preceding and succeeding orbits have a similar pattern, but are horizontally shifted.

Figure 7 (left) shows the footprint locations for one beam cycle during an descending orbit while Figure 7 (right) shows the measurement centers for one side of a descending pass. Figures 8 and 9 show further zoom ins for each beam separately.

The Seasat spacecraft flew in a sun-synchronous circular polar orbit at an inclination of 98.7° and an altitude of $900 \, \mathrm{km}$ (Grantham et al., 1977). During its mission lifetime, it had a 4 day near-repeat orbit, collecting σ^o measurements essentially continuously on both sides of the spacecraft ground track¹. As described below, from these σ^o measurements twice-

¹The instrument operation mode was frequently altered resulting in much reduced HH coverage compared to VV coverage.

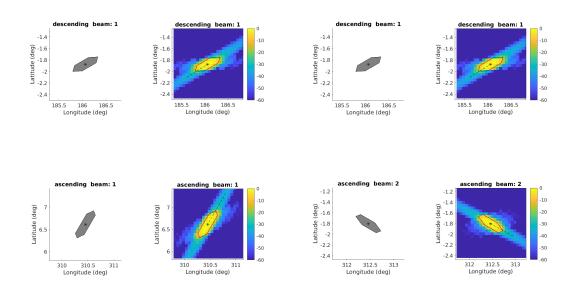


Figure 5: Arbitrarily selected examples of the full spatial gain pattern response of several mid-swath SASS σ^o measurements from different antenna beams. The dashed line shows the along-beam direction. The red, black, and green quadrilaterals show the instantaneous 3-dB footprint for the first, twelfth, and twenty-fifth pulses.

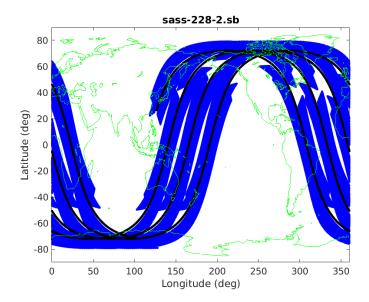


Figure 6: SASS σ^o measurement locations during several orbits. Individual measurements cannot be resolved in this plot.

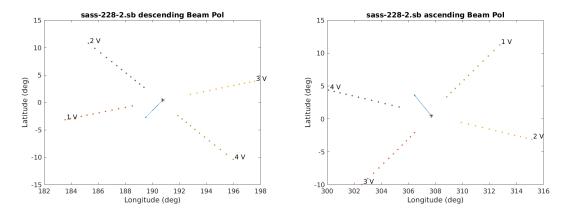


Figure 7: SASS σ^o measurement locations (left) for a particular antenna cycle during an ascending pass, and (right) for multiple pulse cycles zoomed in during a descending pass. The diagonal patterns are the result of missing σ^o measurements due to a calibration cycle, which occurs once per 100 antenna cycles. Each antenna beam is a different color.

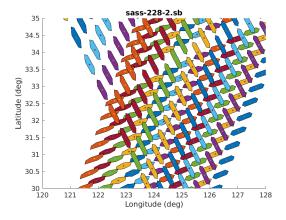


Figure 8: SASS 3-dB σ^o measurement layouts for a forward and an aft looking beam. Colors correspond to the along-beam measurement number. So, a particular color is a fixed cross-track distance from the spacecraft nadir track. These represent the binary response function.

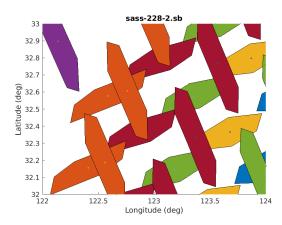


Figure 9: SASS 3-dB σ^o measurement layouts for two beams This is a zoom in of Fig. 8. Colors correspond to the along-beam measurement number. So, a particular color is a fixed cross-track distance from the spacecraft nadir track. These represent the binary response function.

daily global images were created by (1) DIB gridding of the σ^o measurements on a 25 km grid and (2) applying the SIR algorithm to enhance the effective resolution of the data by exploiting the irregular patterns of measurement locations and signal oversampling (from overlaps in adjacent footprints and overlapping swaths). The SIR images are reported on a 3.125 km grid.

4.3 Grid Spatial Extent

Azimuthal *SASS* grids extend to the full Northern (EASE2-N) and Southern (EASE2-S) hemispheres, respectively, as described in Brodzik et al. (2012, 2014) (Fig. 10). The spatial extent of the equal-area cylindrical projections (Fig. 12 and Fig. 11) is defined to match the extent of compatible grids favored by two user communities: the Mid-Latitude (EASE2-M) grid, extending to $\pm 85.044\,566\,4^\circ$ latitude, has been adopted by the SMAP user community; the Temperate and Tropical (EASE2-T) grid, limited to latitudes equatorward of $\pm 67.1^\circ$, is consistent with the original CETB products defined for similar scanning radiometers (Brodzik et al., 2021). See Appendix A Table 7 for grid specifications.

4.4 Grid Spatial Resolution

SASS grid resolutions are defined relative to a SI25km base resolution: $25\,\mathrm{km}$ grids and $3.125\,\mathrm{km}$, which include EASE2-N, EASE2-S and EASE2-T grids that are compatible with the MEaSURES CETB data products (Brodzik et al., 2021). Nested resolutions relative to the CETB $25\,\mathrm{km}$ base grids are defined using exact divisors of 2, as illustrated in Figure 13. SASS projection extents, dimensions and grid cell size details are included in Appendix A. Grids

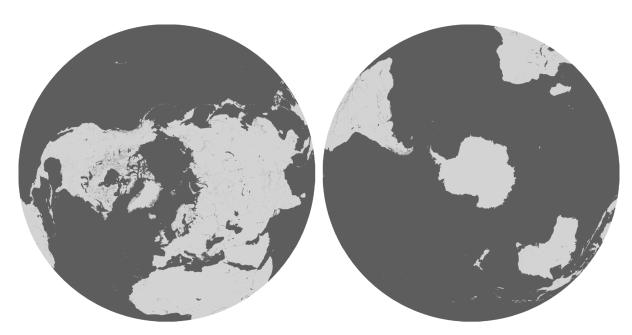


Figure 10: Northern and Southern EASE-Grid 2.0 projection extents. Land-ocean mask from Brodzik and Knowles (2011).

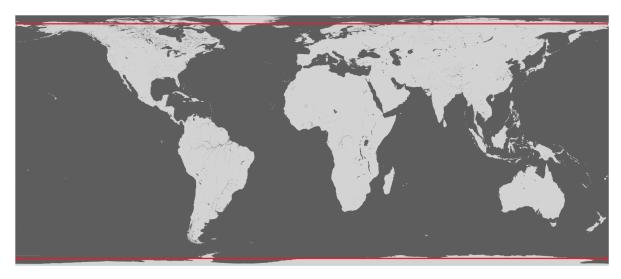


Figure 11: Cylindrical EASE-Grid 2.0 projection extents. Full extent coverage is EASE2-M, with horizontal red lines delineating the smaller latitudinal extent of EASE2-T grid. Land-ocean mask from Brodzik and Knowles (2011).

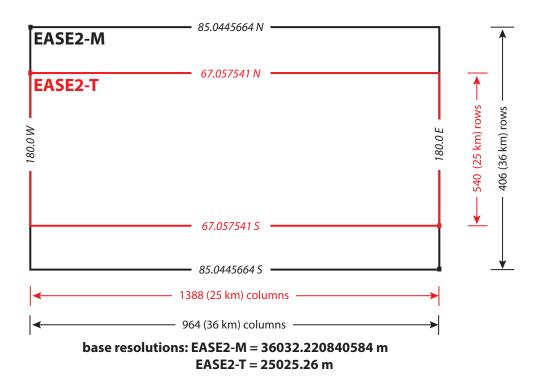


Figure 12: Relationship of EASE-Grid 2.0 cylindrical projection extents. EASE2-T extent is defined for compatibility with CETB products. (Difference in latitudinal extent is exaggerated, see Fig. 11 for actual difference in projected extent. (Brodzik et al., 2021).

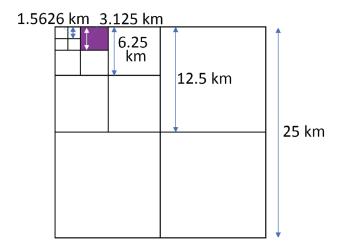


Figure 13: CETB nested grids based on a 25 km base resolution cell. Only 25 km and 3.125 km divisions are used in SASS products (Long et al., 2019).

used for SASS processing are included in Table 4.

Table 4: SASS EASE-Grid 2.0 base grids produced, by projection and reconstruction algorithm. See Section 5 for GRD and sSIR reconstruction details.

EASE2-M	EASE2-N	EASE2-S	EASE2-T
n/a n/a	25km (GRD) 3.125km (GRD/SIR)	25km (GRD) 3.125km (GRD/SIR)	25km (GRD) 3.125km (GRD/SIR)

4.5 Data Products

The SASS data product at the NSIDC DAAC covers the period beginning 14 Sept (doy 258), 1996 through 28 June (doy 179) 1997. No calibration corrections were applied to the data. In creating a time series of times, a "moving average" approach was used with overlapping imaging periods, that start every mission day and extend through the desired 8-, 16- or 32-day period (or to the end of the mission, whichever comes first). Table 5 summarizes available SASS radar backscatter products, which are all in CETB-standard EASE-2 Grid projections.

 Table 5: Available twice-daily SASS image products.

MRF	days	Algo-	Pix. Res.	Regions*	Polar-	Size [†]	
Type		rithm	(km)		ations	N/S/T (MB)	
	8,16,32	GRD	25	N,S,T	HH,VV	3/3/5	
Binary	8,16,32	SIR	3.125	N,S,T	HH,VV	255/225/400	

* Region code: N=Northern Hemisphere, S=Southern Hemisphere, T=Global \dagger Uncompressed size

5 Algorithm Description

5.1 Background

The *effective* resolution of an image is defined by the *pixel spatial response function* (PSRF), with the effective resolution is given by the dimension(s) of one-half power (3-dB) extent of the PSRF. In contrast, the *measurement* response function (MRF) describes the spatial characteristics of the *individual* measurements. For a radar, the MRF depends on the two-way antenna pattern, the modulation, and the signal processing. For both radars and radiometers, the PSRF depends on the MRF and the image formation algorithm. In linear image formation algorithm, the reported pixel value consists of the weighted sum of nearby measurements. In this case the PSRF is then the normalized weighted sum of the measurement MRFfunctions, including their spatial offset from the center of the pixel.

In creating the SASS backscatter image product, multiple measurements from different passes are combined into single pixel values. The resulting image pixels have an effective resolution slightly coarser than the pixel spacing since (a) the measurements are not all centered the same and (b) their MRFs can extend outside of the pixel area. The PSRF provides the tool for defining the effective pixel resolution.

The spacing of pixels is termed the "pixel posting" or the "posting resolution". Note that the posting resolution is not the same as the *effective resolution* which is defined by the PSRF. In general, the effective resolution is coarser than the posting resolution (see (Long and Brodzik, 2016a)). In order to be compatible with the CETB data set, two posting resolutions are considered: 25 km and 3.125 km. See Fig. 14.

5.2 SASS Backscatter Image Products

The SASS backscatter products include both low-noise (low-resolution) coarse resolution GRD images and higher-noise (enhanced) fine-resolution (SIR) images. The various products have their advantages and disadvantages. The multiple images allow users the flexibility of choosing the appropriate images for their research application.

To create radar CETB-compatible products, different approaches are used for each resolution. For GRD images the source backscatter measurements are gridded onto to a 25 km grid using drop-in-the-bucket (DIB) techniques. In this approach, all the measurements whose center falls within a grid element are averaged into the reported value. For the 3.125 km product, the source measurements are processing using the AVE (the first iteration of SIR) and the SIR image algorithms. Along with each measurement's MRF, the SIR algorithm exploits the irregular patterns of measurement locations and signal oversampling (from overlaps in adjacent footprints and overlapping passes).

Because the sensor was not designed as an imager, there are gaps between the measurements that must be filled by combining multiple passes over an extended imaging period.

With a 4 day near-repeat cycle but needing additional passes to provide better coverage, thre imaging periods are defined: 8 day, 16 day, and 12 day. These provide a user-selectable tradeoff between temporal resolution, spatial resolution, and noise.

Table 5 summarizes the image product types. Simple GRD images are created using drop-in-the-bucket (DIB) techniques at 25 km. In DIB, the measurements whose center falls within a given pixel area are averaged. AVE images use weighted averages where the weighting is the measurement MRF, which may vary from measurement to measurement. The SIR algorithm is employed for slice and footprint images on the 3.125 km pixel grid.

5.3 Radar Spatial Response and Image Reconstruction

The effective spatial resolution of an image product is determined by the spatial measurement response function (MRF) of the sensor and by the image formation algorithm used. The MRF is determined by the antenna gain pattern, the scan geometry (notably the antenna scan angle), and the signal processing, see Long et al. (1993), Long (2017). The goal in forming a σ^o image map is to estimate the backscatter properties of the surface from noisy measurements that employ (possibly variable) MRFs that sample the surface. Though simple to implement, DIB techniques ignore the MRF, which limits their effective resolution. Reconstruction techniques that use the MRF can provide much finer effective resolution.

Reconstruction processing techniques effectively assume the underlying signal (the back-scatter) being sampled is band-limited, which is the only consistent assumption possible with sampled data (Long and Brodzik, 2016b, Long and Franz, 2016b). For reconstruction, the backscatter at each point of a fine-scale pixel grid is estimated, producing a backscatter image or map. While the image is generated on a regular grid, the measurement locations and MRF are not aligned with the grid, and so the measurements form an irregular sampling pattern, which can complicate signal reconstruction. Many commonly used image formation algorithms either ignore this (as is done in DIB) or attempt to interpolate or distance-weight the measurements values. In using image reconstruction, we avoid these ad hoc, non-optimal approaches and explicitly compute the MRF of each measurement as part of the reconstruction process. This is computationally intense, but provides the best possible image construction. The remainder of this section outlines this process.

An individual scatterometer backscatter measurement z_i can be modeled as the integral of the product of the MRF and the surface backscatter, i.e.,

$$z_i = \iint MRF_i(x, y; pp)\sigma^o(x, y, \theta, \phi_i, t, pp)dxdy + noise$$
 (1)

where $\mathrm{MRF}_i(x,y;pp)$ is the spatial MRF of the ith measurement at x,y and the surface σ^o depends on spatial location x,y, incidence angle θ , azimuth angle ϕ , time t, and polarization

pp, i.e.,

$$MRF_{i}(x, y; pp) = \iint \frac{G_{a}^{2}(x, y; pp)G_{p}(x, y; pp)}{R^{4}(x, y)}.$$
 (2)

where

$$X = \iint \frac{G_a^2(x, y; pp)G_p(x, y; pp)}{R^4(x, y)} dx dy.$$
(3)

where $G_a(x,y;pp)$ is the effective two-way antenna gain at the surface at (x,y) for polarization pp, $G_p(x,y;pp)$ is the processor gain, and R(x,y) is the slant range from the radar to the surface. Note that the measurement is an average of σ^o in spatial coordinates as well as in azimuth and incidence angles.

Eq. 1 is discretized on the imaging grid to become

$$z_i = \sum_{j \in \text{image}} h_{ij} a_j + \text{noise}$$
 (4)

where a_j is the backscatter at the center of the j^{th} pixel at (x_l, y_k) and $h_{ij} = MRF(x_l, y_k; \phi_i)$ is the discretely sampled MRF for the i-th measurement evaluated at the j-th pixel center where h_{ij} is normalized so that $\sum_j h_{ij} = 1$. In practice, the MRF is negligible some distance from the measurement center, so the sums need only be computed over a small area around the pixel. Ignoring the noise, Eq. 4 can be written as the matrix equation

$$\vec{Z} = \mathbf{H}\vec{a} \tag{5}$$

where H contains the sampled MRF for each measurement and \vec{Z} and \vec{a} are vectors composed of the measurements z_i and a_j , respectively. Even for small images, H is large and sparse, and may be over-determined or under-determined depending on the number and locations of the measurements. Reconstruction of the surface σ^o is equivalent to inverting Eq. 5.

The iterative SIR algorithm (Early and Long, 2001, Long et al., 1993) is a particular reconstruction algorithm that is specifically developed for scatterometer image formation. SIR approximates a maximum-entropy solution to an under-determined equation and a least-squares solution to an over-determined system. The first iteration of SIR is termed 'AVE' (for weighted AVErage) and provides a simple reconstruction estimate that is refined in later SIR iterations. The AVE estimate of the *j*-th pixel is given by

$$a_j = \frac{\sum_i h_{ij} z_i}{\sum_i h_{ij}} \tag{6}$$

where the sums are over all measurements that have non-negligible MRF at the pixel. The SIR iteration begins with an initial image a_j^0 whose pixels are set to the AVE values defined in Eq. 6. Thereafter, the iterative equation for single-variate SIR is given by

$$a_j^{k+1} = \frac{\sum_i u_{ij}^k h_{ij}}{\sum_i h_{ij}}$$
 (7)

where

$$u_{ij}^{k} = \begin{cases} \left[\frac{1}{2p_{i}^{k}} \left(1 - \frac{1}{d_{i}^{k}} \right) + \frac{1}{a_{j}^{k} d_{i}^{k}} \right]^{-1} & d_{i}^{k} \ge 1\\ \frac{1}{2} p_{i}^{k} (1 - d_{i}^{k}) + a_{j}^{k} d_{i}^{k} & d_{i}^{k} < 1 \end{cases}$$
(8)

$$d_i^k = \left(\frac{z_i}{p_i^k}\right)^{\lambda} \tag{9}$$

where $d_i^k = (s_i/p_i^k)^\lambda$ with $\lambda = \frac{1}{2}$. The factor d_i^k is the square root of the ratio of a measurement to its forward projection at the k^{th} iteration. The update term u_{ij}^k is a non-linear function of both d_i^k and the previous image a_j^k . The sigmoid-like non-linearity in Eq. 8 constrains the amount of change permitted during any one iteration, thereby minimizing the effects of noise Long et al. (1993). Though not used in this paper, a spatial median filter can be applied to the image between iterations to further reduce the noise Long et al. (1993).

For scatterometers, SIR is implemented in dB (Long, 2017, Early and Long, 2001, Long et al., 1993); i.e., the computation is done on $10\log_{10}(z_i)$ rather than on the linear-space value z_i as done in the radiometer version of SIR (Long and Brodzik, 2016a, Long and Daum, 1998). In considering the differences between linear and dB processing, recall the well-known fact that computing the arithmetic mean of values in dB is equivalent to computing $10\log_{10}$ of the geometric mean of the linear-space values (Wikipedia, 2016). With the measurements in dB, the reconstruction processing can be viewed as a form of weighted geometric mean filtering. Since it has been found that geometric mean filters are better at reducing Gaussian-type noise and preserving linear features than (linear) arithmetic mean filters (Pitas and Venetsanopoulos, 1986), some performance advantage to dB processing is expected and observed (Long, 2017). The linear and dB computations yield similar, but slightly different results, due to the varying signal-to-noise ratio (SNR) of the measurements and limited signal dynamic range (Long, 2017).

In practice, since the σ^o measurements are quite noisy, attempting full image reconstruction can produce excessive noise enhancement. In general, more iterations improve the signal and resolution, but also increase the noise level. To reduce noise enhancement and resulting artifacts, regularization can be employed, at the expense of resolution (Long and Franz, 2016a, Early and Long, 2001, Long et al., 1993, Long, 2017). Regularization is a smoothing constraint introduced in an inverse problem to prevent extreme values or overfitting. Regularization results in partial or incomplete reconstruction of the signal (Long and Franz, 2016a). It also creates a trade off between signal reconstruction accuracy and noise enhancement. SIR includes regularization achieved by prematurely terminating the iteration. Based on simulations and confirmed by analysis of actual data, 20-30 iterations provides a nice trade off result. We note that for a noisy sensor like a scatterometer, the results are not particularly sensitive to the precise value chosen, hence a fixed value can be selected. Selection of the number of iterations is based on simulation, see citeearly2001,

Long et al. (1993) and Long (2017). For this product, a fixed (30) number of SIR iterations is employed for both binary and full response MRFs.

5.3.1 Local-Time-of-Day

As previously noted, the goal of image reconstruction is to estimate the surface σ^o from the sensor σ^o measurements. Measurements from multiple orbit passes over a narrow local time window are combined. When multiple measurements are combined, the resulting images represent a temporal average of the measurements over the averaging period. There is an implicit assumption that the surface characteristics remain constant over the imaging period For both conventional-resolution (GRD) and enhanced-resolution (SIR) images.

The radar backscatter of a natural surface is a strong function of the state of the water it contains, i.e., frozen or thawed. As a result of the sun-synchronous orbit geometry, the radar observations at a given location on the earth fall within two narrow diurnal windows. At the equator, these correspond to the ascending and descending orbit passes. This can be exploited to provide twice-daily sampling. Thus, *SASS* images on the cylindrical *EASE-Grid 2.0* projections are separated by ascending and descending passes. A separate image ("both") product is also made that combines both which achieves between spatial coverage at the expense of temporal resolution.

Near the poles, the temporal windows widen to several hours but remain relatively narrow. Since surface temperatures can fluctuate widely during the day, daily averaging is not generally useful at these locations, since it smears diurnal temperature fluctuations in the averaged σ^o . However, it is reasonable to split the data into two distinct images per day, using intervals based on local-time-of-day (ltod), thereby only combining measurements with a similar ltod. This minimizes the fluctuations in the observed backscatter at high latitudes due to changes in physical temperature from daily temperature cycling.

The SASS images on the azimuthal projections are separated into twice-daily, morning and evening passes based on observation ltod, in addition to images that combine the two. At low latitudes, which typically have few overlapping swaths at similar ltod in the same day, ltod division is equivalent to ascending/descending division. An ancillary data array is included in each file, to describe the effective time average of the measurements combined into the pixel for a particular day. This enables investigators to explicitly account for the ltod temporal variation of the measurements included in a particular pixel. A separate image ("both") product is also made that combines both which achieves greater spatial coverage at the expense of temporal resolution.

Histograms of the ltod of the sensor's measurements falling within two narrow latitude bands are shown in Fig. 15. For the SASS orbit, a natural division in the measurement ltod is at 00:00 and 12:00 h. For consistency with Long and Brodzik (2016b) and Brodzik et al. (2021), the SASS data are produced using this ltod division. Note how the ltod falls within one of two tight groups that correspond to the ascending and descending orbit passes, and

that there are natural divisions in the measurement ltod at 00:00 and 12:00 hrs. Thus, the measurements provide twice-daily sampling. Note that when more than day's worth of data, the ltod division is maintained so that a multi-day morning image combines only morning observations.

5.4 Sample Data

Figures 16–18 present examples of 8-day product images for each polarization and region where all passes ('both') within the imaging period are combined. Swath-like artifacts over the oceans are the result of significant temporal variation of surface σ^o due to wind changes during the imaging interval. Over the ocean high winds correspond to higher σ^o values while low winds correspond to low wind speeds. Additional data visualization are provided in later sections.

Table 6: Study Sub Regions

Region	Longitude		Latitude		A_{HH}	B_{HH}	A_{VV}	B_{VV}
	left	right	lower	upper	dB	dB/deg	dB	dB/deg
Amazon	294	295.5	-6	-4	-7.12	-0.0684	-7.47	-0.0836
Congo	19	21.5	-1.5	1.25	-6.63	-0.0486	-7.08	-0.0677
Greenland (large)	317	328	75	79	-5.17	-0.1813	-4.32	-0.1347
Greenland* (small)	312	328	70	70.25	_	_	_	_
Pampas	299	300	-37	-35	-10.82	-0.1468	-11.53	-0.1359

^{*}Each small Greenland subregion spaced 2 deg of longitude has longitude extent 0.5 deg

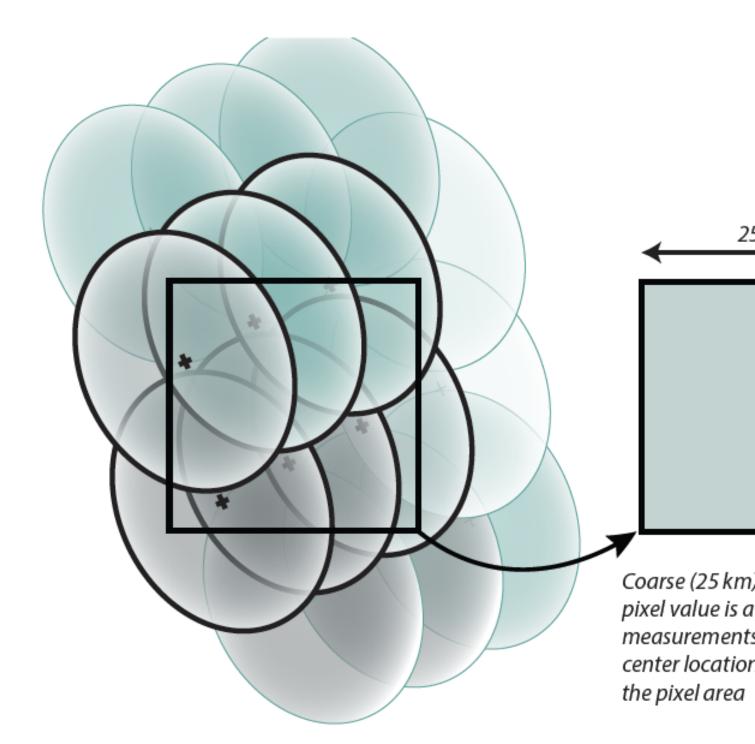
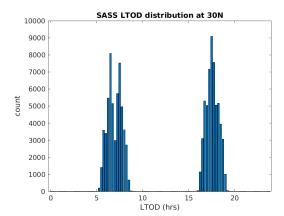


Figure 14: Conceptual illustration of coarse 25 km (left) vs. high resolution 3.125 km (right) pixels. The ellipses represent the individual MRFs of the measurements. (The actual shapes are more complicated than this.) DIB is used for GRD imaging while AVE and SIR are used for high resolution images.



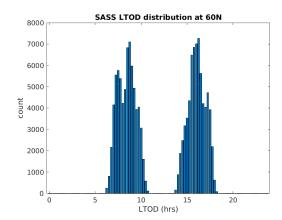


Figure 15: Histograms of typical measurement Itod for SASS measurements falling within a 1° latitude band at (left) $30^{\circ}-31^{\circ}$ N and (right) $60^{\circ}-61^{\circ}$ N over one day. All measurements fall into essentially one of two narrow Itod time periods, centered at approximately 00:00 h and 10:00 h in the Northern Hemisphere. Although the center time varies with latitude, any point on Earth is observed at one of two times within ± 90 min.

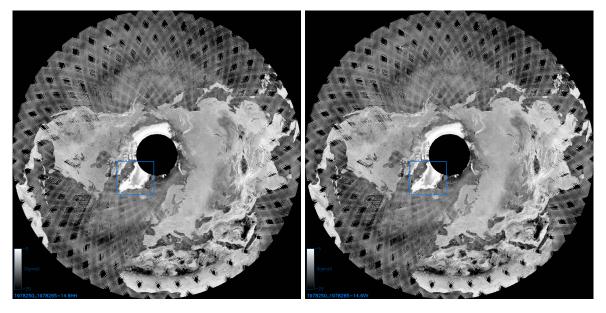


Figure 16: Visualizations of examples of 16-day (doy 2250-265, 1978) SASS A (σ^o at 40° incidence angle) for (left) VV and (right) HH polarizations. Images have been reduced in resolution for presentation here. The large Greenland study area is outlined. See captions for Figs. 18 and 19.

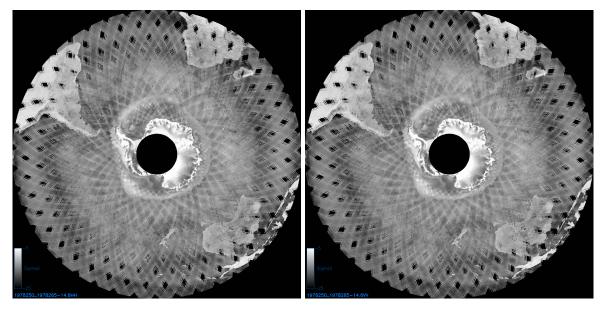
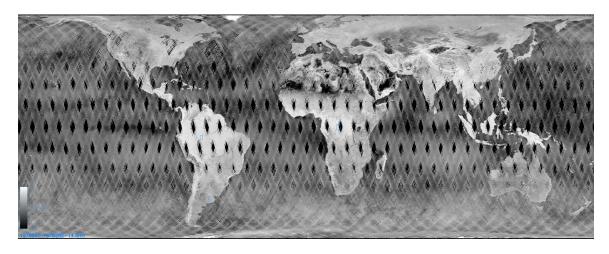


Figure 17: Visualizations of examples of 16-day (doy 250-265, 1978) SASS A (σ^o at 40° incidence angle) for (left) VV and (right) HH polarizations. Images have been reduced in resolution for presentation here.



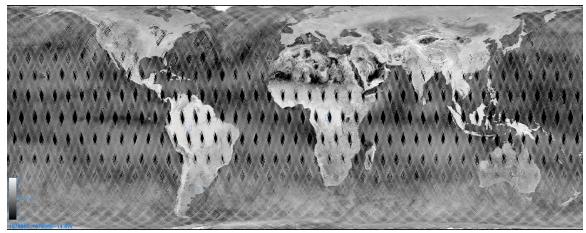


Figure 18: Visualizations of examples of 16-day (doy 250-265, 1978) SASS A (σ^o at 40° incidence angle) for (top) VV and (bottom) HH polarizations. Images have been reduced in resolution for presentation here. Blue boxes show study regions used later. Dark grey diamonds are areas not covered during the imaging interval.

6 Measurement Modeling

To dive deeper into the backscatter data and the performance of the imaging algorithms, we define a number of study regions in Greenland, see Fig. 19 and Tab. 6. The coastal region is employed to visualize the differences between the products at fine resolution in Figs. 20–24.

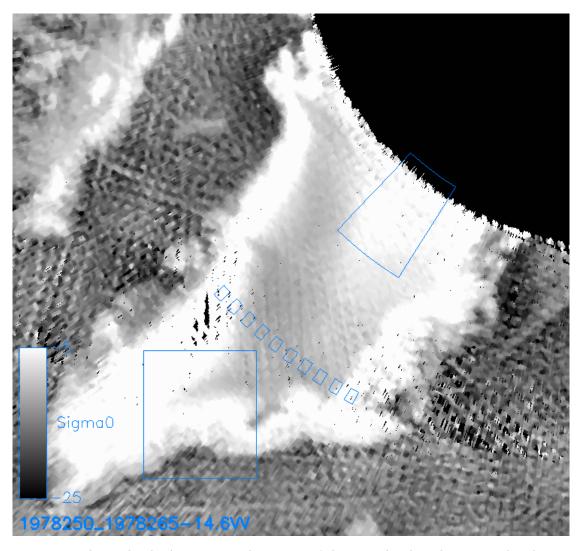


Figure 19: Sample 16 day both pass VV pol A image of the Greenland study area outlined in Fig. 16. Subregions considered in later figures are outlined, see Tab. 6. Note the lack of coverage above $\sim 78^{\circ}$ N.

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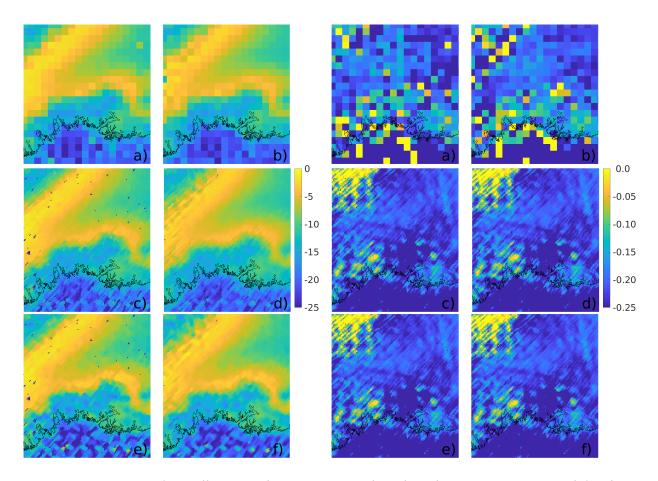


Figure 20: Comparison of HH all-pass 8 (doy 210-217) and 16 day (doy 206-221), 1978. (left side) A in dB. (right side) B in dB/deg. (a) 8-day 25 km pixel GRD. (b) 16-day 25 km pixel GRD. (c) 8-day 3.125 km pixel AVE. (d) 16-day 3.125 km pixel AVE. (e) 8-day 3.125 km pixel SIR. (f) 16-day 3.125 km pixel SIR. Black spots in the binary response images are pixels not included in the coverage. Texture artifacts result from limited measurement overlap and coverage during the imaging interval, which are more severe for H-pol.

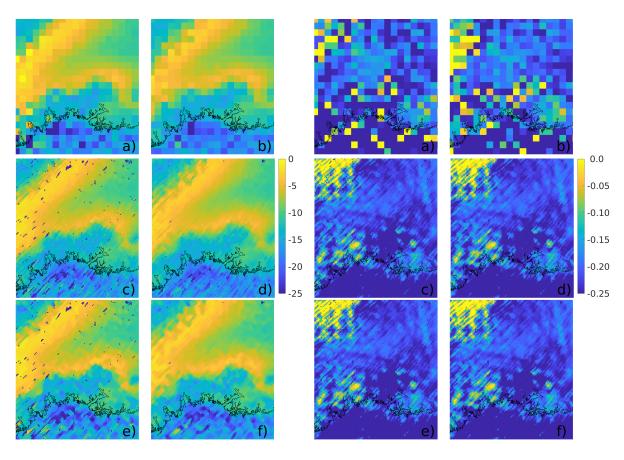


Figure 21: Comparison of VV all-pass 8 (doy 210-217) and 16 day (doy 206-221), 1978. (left side) A in dB. (right side) B in dB/deg. (a) 8-day 25 km pixel GRD. (b) 16-day 25 km pixel GRD. (c) 8-day 3.125 km pixel AVE. (d) 16-day 3.125 km pixel AVE. (e) 8-day 3.125 km pixel SIR. (f) 16-day 3.125 km pixel SIR. Black spots in the binary response images are pixels not included in the coverage. Texture artifacts result from limited measurement overlap and coverage during the imaging interval.

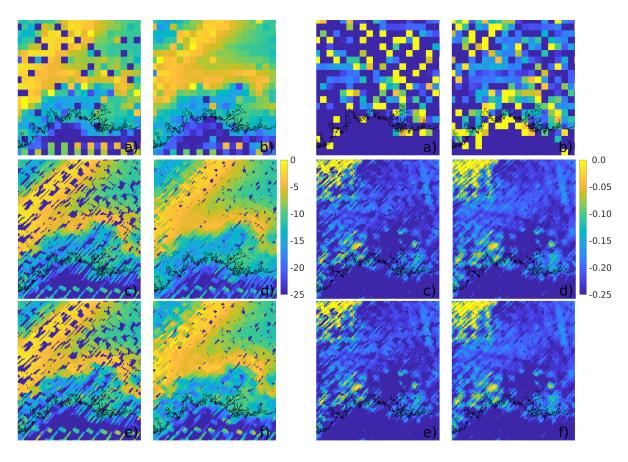


Figure 22: Comparison of HH evening-pass (doy 210-217) and 16 day (doy 206-221), 1978. (left side) A in dB. (right side) B in dB/deg. (a) 8-day 25 km pixel GRD. (b) 16-day 25 km pixel GRD. (c) 8-day 3.125 km pixel AVE. (d) 16-day 3.125 km pixel AVE. (e) 8-day 3.125 km pixel SIR. (f) 16-day 3.125 km pixel SIR. Black spots in the binary response images are pixels not included in the coverage. Texture artifacts result from limited measurement overlap and coverage during the imaging interval, which are more severe for H-pol.

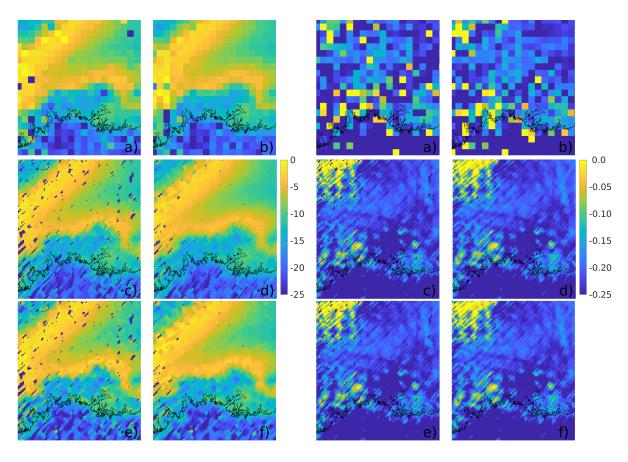


Figure 23: Comparison of HH morning-pass 8 (doy 210-217) and 16 day (doy 206-221), 1978. (left side) A in dB. (right side) B in dB/deg. (a) 8-day 25 km pixel GRD. (b) 16-day 25 km pixel GRD. (c) 8-day 3.125 km pixel AVE. (d) 16-day 3.125 km pixel AVE. (e) 8-day 3.125 km pixel SIR. (f) 16-day 3.125 km pixel SIR. Black spots in the binary response images are pixels not included in the coverage. Texture artifacts result from limited measurement overlap and coverage during the imaging interval, which are more severe for H-pol.

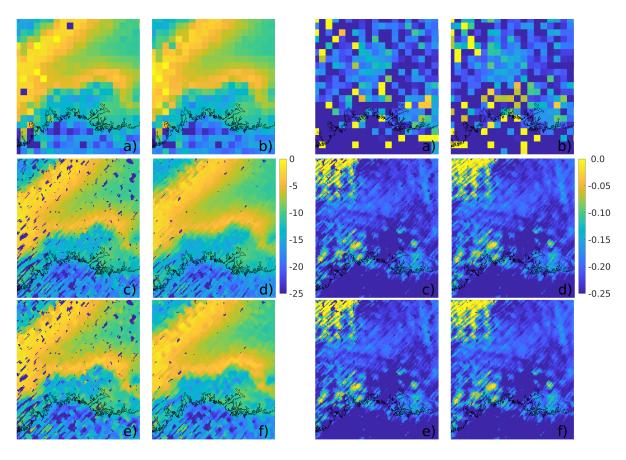


Figure 24: Comparison of VV morning-pass 8 (doy 210-217) and 16 day (doy 206-221), 1978. (left side) A in dB. (right side) B in dB/deg. (a) 8-day 25 km pixel GRD. (b) 16-day 25 km pixel GRD. (c) 8-day 3.125 km pixel AVE. (d) 16-day 3.125 km pixel AVE. (e) 8-day 3.125 km pixel SIR. (f) 16-day 3.125 km pixel SIR. Black spots in the binary response images are pixels not included in the coverage. Texture artifacts result from limited measurement overlap and coverage during the imaging interval.

6.1 Incidence Angle Effects

Over natural surfaces σ^o depends on the measurement incidence angle. Since SASS is a fanbeam system, it collects σ^o measurements over a range of incidence angles ranging from about 15° to 60° . The variation in incidence angle must be accounted for when combining multiple measurements. The incidence angle normalization $\gamma^o = \sigma^o/\cos\theta$ where θ is the incidence angle is sometimes used. However, the slope of this correction is strictly downward and since upward slopes are observed in some areas, this normalization is not used. Instead, following prior investigators (see Long et al. (1993) and references therein) a linear slope is used that is centered at 40° , i.e., σ^o as a function of incidence angle is modelled according to

$$\sigma^o = A + B(\theta - 40^\circ) \tag{10}$$

where A is σ^o at 40° incidence angle; B is the slope of σ^o versus incidence angle θ . At each pixel, the model parameters A (the mean σ^o), B (the normalized slope of σ^o versus incidence angle are estimated from the backscatter measurements on a pixel by pixel basis.

Note that there is a variation (typically <1°) in incidence angle over the the footprint of each measurement. Because the measurements integrate the echo return over the measurement MRF, only a single σ^o , mean incidence angle, and mean azimuth angle value is reported for an SASS measurement. The measurements essentially average the incidence and azimuth angle dependence over the MRF. While the *intra*-measurement angle variation is small, the *inter*-measurement the variation in incidence angle between measurements is much larger, and has a significant effect.

To explore this, some small $(0.5^{\circ}$ longitude by 0.25° latitude) study regions are defined in the Greenland Ice Sheet, see Fig. 19. The regions are individually small enough to have nearly spatially constant scattering characteristics, but span the range of ice facies Long and Drinkwater (1994) over the ice sheet with a variety of mean σ^{o} values. Figures 25 and 26 shows the variation in incidence angle for measurements collected over each of these study regions during a 41-day interval. Noting the sloping dependence of σ^{o} (and γ with incidence angle. Linear least-squares (in both linear space and with σ^{o} in dB) fits of σ^{o} versus incidence angle are shown as solid lines. The coefficients of the the linear (σ^{o} in dB) fit are included in Tab. 6. In Fig. 26 scaled coefficients of the fits (in dB) are included as overprinted values. In each panel, the top line is linear fit with A (the mean value at 40 deg incidence angle) on the left and B (the slope) times 10 on the right. The second line shows the coefficients of the quadratic fit with A on the left, B times 10 in the center and C times 1000. The third line is the coefficients of the cubic fit with A on the left, B times 10 left of center, C times 1000 right of center and D times 10000 on the right where

$$\sigma^{o} = A + B(\theta - 40) + B(\theta - 40)^{2} + C\theta - 40)^{3}.$$
 (11)

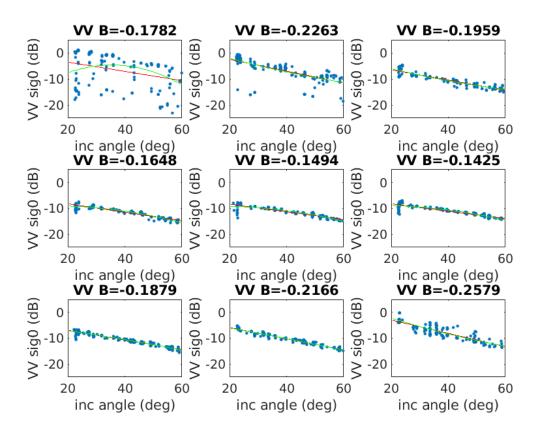


Figure 25: Vertically-polarized σ^o versus incidence angle for Greenland sub regions showing (red) σ^o in dB linear fit and (green) σ^o and (green) σ^o in normal space (not dB) linear fit to the data. Panel titles give the slope B in dB/deg for the σ^o in dB model. Because of the small sub region size, data from the entire mission was used. Refreezing of firn in areas some regions result in two different populations of data over long time interval.

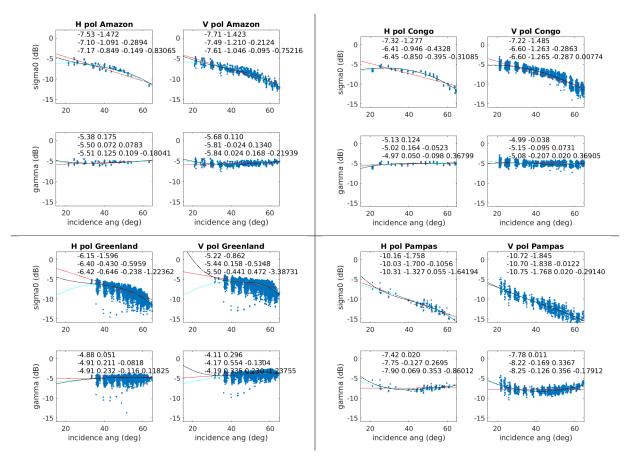


Figure 26: σ^o and γ versus incidence angle for four study regions of varying locations and size with different surface types showing (red) linear, (green) quadratic, and (black) cubic σ^o in dB versus incidence angle fits to the data. Data is from the entire mission, all passes. See text regarding numbers on plot.

6.2 Azimuth Angle Effects

Periodic natural surfaces exhibit variations in σ^o with azimuth angle, including water waves Ulaby and Long (2014), Naderi et al. (1991), sastrugi and snow dunes (Long and Drinkwater, 2000, Lindsley and Long, 2016, Ashcraft and Long, 2006). The measured σ^o is thus a function of the azimuth direction from which the surface is observed. Scatterometers such as SASS are *designed* to make multi-azimuth observations over the ocean to exploit this effect for wind-driven wave in order to estimate the near-surface wind Naderi et al. (1991). However, these measurements intrinsically coarse since they must be made in a single pass. Unlike the ocean, land and ice features do not (generally) change as rapidly so observations from multiple passes can be combined.

Over the course of the orbit's repeat cycle each point on the surface can be observed at multiple azimuth angles. For example, as the spacecraft passes over a particular location within the swath, the location is first observed looking, then a short while later the same location is observed looking backward. Over the orbit repeat cycle, the ground track shifts so that the same location is observed from a different set of azimuth angles for each pass. The precise distribution of azimuth angles depends on the orbit latitude, with the narrowest range near the equator and the largest range at high latitudes.

Note that there is a trade off between the imaging time period, the spatial resolution, and the azimuth sampling. Short time periods provide better temporal resolution for tracking sea ice motion and rapid freeze thaw events. However, short time periods provide inadequate coverage and/or azimuth sampling to reliably estimate the azimuth angle variation, particularly when the data is divided by local time of day. Recalling that the orbit repeat cycle is near-repeat after 4 days, we choose N_d =4 and N_d =8 day imaging intervals (N_d in days². The imaging intervals are chosen to overlap by N_d – 1 days so they act like a N_d long moving average filter. Shorter N_d provides finer temporal resolution at the expense of reduced spatial coverage/resolution, including possible spatial artifacts in the reconstruction. These negative effects are reduced for the longer imaging intervals.

Note that a particular σ^o observation is an average of σ^o in spatial coordinates as well as in azimuth and incidence angles. Within a single measurement the azimuth angle span (<1°) for a particular measurement is small and can be neglected. The incidence angle span within a single measurement can be slightly larger (1-1.5°). The roll off of σ^o versus incidence angle, slightly biases the integrated measurement toward smaller incidence angles. This effect is neglected.

On the other hand, the variation in σ^o as a function of azimuth and incidence angles for different measurements is important and provides useful geophysical information. Incidence angle variation is considered in the previous section. Of cource, the variation in σ^o as a function of azimuth is what enables wind retrieval over the ocean (Ulaby and Long,

²Imaging intervals are specified in days, but may include only morning or evening (or descending or ascending) passes depending on the ltod setting.

2014, Meissner et al., 2017). Azimuth variation (sometimes termed 'azimuth modulation') can be observed over snow dunes and sastrugi (Long and Drinkwater, 2000, Ashcraft and Long, 2006, Lindsley and Long, 2016) and sand dunes in ergs³ (Stephen and Long, 2007). As a result, significant azimuth variation in σ^o is common over the Great Ice Sheets (GI) of Greenland and Antarctica, but is only rarely observed elsewhere over large regions with the exceptions of ergs.

For fan-beam scatterometers, since each satellite pass observes a given point on the surface from a limited azimuth angle, the variation of σ^o with azimuth can lead to biases in the mean σ^o value and to imaging artifacts when multiple passes with different azimuth angle observations are combined. To deal with azimuth variation of σ^o on the GI, previous investigators, e.g., Long and Drinkwater (2000) Ashcraft and Long (2006), and Lindsley and Long (2016), have used a simple Fourier series model for the azimuth variation observed in σ^o . Two models have been considered. One (here termed 'FA') with fixed azimuth modulation coefficients and the other (here termed 'VA') with incidence angle-dependent azimuth modulation coefficients. The azimuth modulation models can be expressed as

$$\sigma^0 = A + B(\theta - 40) + M_1 \cos(\phi + P_1) + M_2 \cos(2\phi + P_2)$$
(12)

where ϕ is the azimuth angle, $M_1 = A_1$ and $M_2 = A_2$ for the FA model, and $M_1 = A_1 + R_1(\theta - 40)$ and $M_2 = A_2 + R_2(\theta - 40)$ for the VA model where A_1 and A_2 are the mean azimuth modulation coefficients and P_1 and P_2 are the phase angles relative to north. Note that the model can be with σ^o in dB or linear space, though dB model have proven to the the most successful (Long and Drinkwater, 2000, Lindsley and Long, 2016).

Unfortunately, with a maximum of 4 azimuth angles, the SASS geometry is not very well suited for estimating the azimuth variation. Further, in the polar regions the incidence angle and azimuth angle of the observations at a given point may be coupled for fan-beam scatterometers, which greatly complicates azimuth dependence estimation (Long and Drinkwater, 2000). Thus, for this product azimuth dependence is ignored.

6.3 Binary Versus Full Response Images

In creating the CETB SASS radar product, separate images products were generated using the binary approximation and the full MRF. There are advantages to both approach, so the user must select which is the most appropriate for their study. This section is provided to further understand the tradeoffs between the two MRF options. See Section 4.2 for the details on the two MRF options.

³An erg landform is a large region or 'sea' of vegetation-free, wind-swept desert sand.

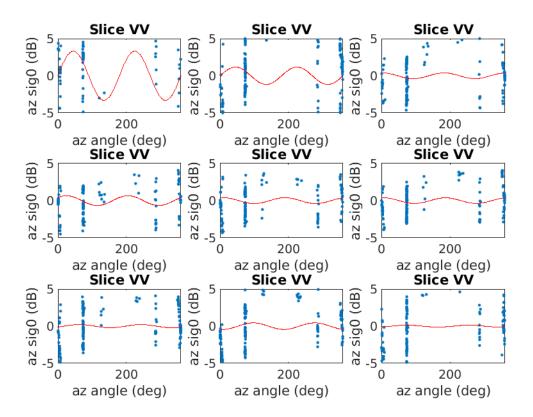
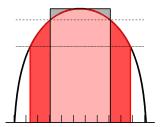
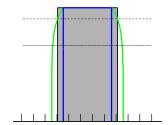


Figure 27: σ^o versus azimuth angle relative to north for Greenland subregions with 1st order azimuth modulation fit shown in red. Individual σ^o measurements have been corrected for incidence angle and adjusted to zero mean. The individual plots are for the sub regions within the larger Greenland study area. The noisy measurements and limited azimuth sampling preclude accurate estimates of the azimuth variation.





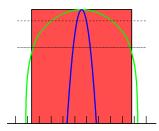


Figure 28: Notional plots of binary and full response MRFs and corresponding PSRFs for one and multiple measurements using AVE. In these one-dimensional illustrations only the main lobe of the MRF is shown. (left) Solid black line shows the true normalized MRF in dB versus distance. The gray box is the binary (1/0) rect-function approximation. The red line the full response MRF used, which is the full response MRF that is truncated to some threshold value (-10dB in this example). (center) Effective PSRF estimate when the binary approximation is used. The gray box is the result when only a single measurement is available. The green line corresponds to the PSRF estimate when a dense set of measurements are available when the image formation is done in linear (not dB) space. The blue line corresponds to the PSRF estimate when a dense set of measurements are available when the image formation is done in dB space. (right) Effective PSRF estimate when the truncated full MRF is used. The red box is the result when only a single measurement is available. The green line corresponds to the PSRF estimate when a dense set of measurements are available when the image formation is done in linear (not dB) space. The blue line corresponds to the PSRF estimate when a dense set of measurements are available when the image formation is done in dB space. In all the plots, the upper dashed line is the half-power (-3dB) level below the peak value at OdB. The dash-dot line is the -10dB level. The small lines illustrate spacing of the fine resolution pixels the final image is reported in.

As described in Section 5.1, the PSRF is defined by the weighted combination of the MRFs of the measurements included in the pixel value. The weighting is determined by the choice of the algorithm used to create the image. This can be illustrated with the notional plots in Fig. 28 for AVE.

Unfortunately, the SASS measurement sampling does not fully cover the surface in a single pass, i.e., the surface is undersampled, so there areas of pixels with only a single measurement available. For this case, the AVE (and therefore the SIR) image can only report this measurements' value over the area of its non-zero MRF and no resolution improvement occurs. In fact, depending on the choice of the MRF used in the imaging process (i.e., binary or full response), the reported image has a different effective resolution. As illustrated in Fig. 28, when only a single measurement is available, the binary response results in the smallest area whereas the full response results in a wider span of pixels assigned the value of the measurement, compare the horizontal extents of the gray and red boxes in center and right panels of Fig. 28. Thus, in sparely covered areas, the binary response can be thought

of as having more compact resolution compared to the full response, but the full response may better fill in gaps between measurements.

In contrast, when multiple overlapping measurements are available, i.e., the surface is oversampled, it is possible to obtain finer effective resolution. This is seen by comparing the the blue PSRFs in center and right panels of Fig. 28. The multi measurement PSRF was computed by summing the MRFs of a dense set of measurements and normalizing. This summation can be done in linear space (i.e., not in dB) or in dB. As noted in Section 5.3, the latter is used for SIR. The improvement in resolution (narrowing of the width) of the PSRF compared to the MRF is apparent.

Enhancement of the effective resolution *requires* dense sampling of the surface. This is the reason multiple passes are used. In addition, multiple measurements at a diversity of incidence angles are required to estimate the incidence angle slope. When the surface is adequately sampled, the effective spatial resolution is improved which can result in a reduction in noise. However, when the surface is undersampled, it is difficult for the image resolution to be much better than the MRF resolution.

SASS HH-pol images are more frequently undersampled than VV-pol images, particularly for 8 day images made separately for morning and evening. Undersampling is less frequent for 16 and 32 day images, particularly for the "B" all pass case.

6.4 Data Volume

Table 5 summarizes available CETB SASS radar products, which are all in CETB-standard EASE-2 Grid projections. In this table, "days" refers to the length of time used for image formation. Imaging periods overlap, with a new image started each day. Note that for Itod images that in order to have the right number of morning or evening passes, the time period of the measurements actually used in the images may extend slightly outside the multi-day period. Individual file sizes vary due to internal file compression for each image type. See Section 4.5 for access details.

7 Acknowledgements

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Appendices

A SASS Projections and Grids

Table 7: SASS 25 km product EASE-Grid 2.0 projections and grid dimensions, produced for compatibility with CETB ESDR data products (Brodzik et al., 2021).

Name	Projection	Resolution (km)	Cols	Rows	Latitude Ex- tent	Longitude Extent
EASE2-T25km	Temperate and Tropical Cylindrical	25.025 260 00	1388	540	$\pm 67.0576406^{\circ}$	±180°
EASE2-T3.125km	Temperate and Tropical Cylindrical	3.128 157 50	11 104	4320	$\pm 67.0576406^{\circ}$	±180°
EASE2-N25km	Northern Lambert Azimuthal	25.0	720	720	0°-90°	±180°
EASE2-N3.125km	Northern Lambert Azimuthal	3.125	5760	5760	0°–90°	±180°
EASE2-S25km	Southern Lambert Azimuthal	25.0	720	720	-90°-0°	±180°
EASE2-S3.125km	Southern Lambert Azimuthal	3.125	5760	5760	-90°-0°	±180°

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B SASS Data Definition

B.1 File Requirements

Following Brodzik et al. (2021), SASS product file requirements include:

- Output file format shall be acceptable for NSIDC DAAC to easily ingest to ECS
- File size maximum will be $< 1\,\mathrm{GB}$ (larger files are allowed in ECS, but fast network speeds cannot always be assumed)
- Files will conform to netCDF-CF 1.6 conventions for all but the requirement that puts the lat/lon arrays into the file; however, we will include CF-compliant coordinate variables with projected coordinate locations
- Files should pass CF-compliance-checking for all but the lat/lon arrays (we used JPL compliance-checker)
- Each file will contain 1 or more array variables, with associated ancillary variables, possibly different ancillary variables for each gridding technique. We may have a practical limit on the number of ancillary variables to include, limited by maximum file size
- Each file of the same type (GRD or SIR) will contain the same file-level metadata for that type.
- We will follow the DRY (Don't Repeat Yourself) principle: Metadata will not be duplicated at multiple places in the same file
- DRY exception: Time values will be machine- and human-readable
- DRY exception: Some projection metadata may be in multiple forms (a proj4 string and/or a WKT string)
- Variable/attribute names will be CF-compliant whenever possible

The SASS .nc files work with gdal utility, gdal_translate, to produce a geoTIFF version of each of the data variables <variable_name> in the file, (details in Brodzik et al. (2018)), for e.g.:

```
$ gdal_translate -of GTiff -b 1 \
NETCDF:"cetb.nc":<variable_name> variable_name.tif
```

B.2 Filename Convention

SASS data are distributed by the NSIDC DAAC (http://nsidc.org/data/nsidc-TBD). Filenames are:

```
channel_id>-<-<pre>-<input_source>-<version>.nc
where parts of the filename are described in Table 8.
```

Part	Description	Values	
<pre><pre>cproduct_id></pre></pre>	NSIDC unique data product id	NSIDC-TBD	
<grid_name> <platform> <sensor> <yyyyddd> <channel_id></channel_id></yyyyddd></sensor></platform></grid_name>	EASE-Grid 2.0 grid id Satellite platform Sensor name Date Channel (frequency in GHz and polarization)	See Table 7 Seasat SASS 4-digit year and 3-digit day-of-year 14.6 followed by polarization, one of: • HH = horizontal-horizontal • VV = vertical-vertical	
<pass></pass>	Pass direction (T grids) or ltod (N or S grids)	 one of: B = Both (all measurements) A = Ascending D = Descending M = Morning E = Evening 	
<algorithm></algorithm>	Reconstruction algorithm	one of GRD or SIR	
<version></version>	Version number	production version number	

Table 8: SASS file naming convention

B.3 File Content, v1.0

The following is a sample NetCDF ncdump - h utility output for a SASS v1.0 3.125 km SIR file. File-level metadata and processing details vary depending on projection, spatial resolution and processing details (method, input file list, etc.).

```
netcdf BYU-SASS-EASE2_N3.125km-Seasat_SASS-1978270_1978277-14.6VV-B-SIR-v1.0 {
   dimensions:
   time = UNLIMITED ; // (1 currently)
   y = 5760 ;
   x = 5760 ;
   variables:
   double time(time) ;
   time:standard_name = "time" ;
   time:coverage_content_type = "coordinate" ;
   time:long_name = "ANSI date" ;
```

```
time:units = "days since 1972-01-01 00:00:00";
time:calendar = "gregorian" ;
time:axis = "T";
time:valid_range = 0., 1.79769313486232e+308;
double y(y);
y:standard_name = "projection_y_coordinate" ;
y:coverage_content_type = "coordinate" ;
y:long_name = "y" ;
y:units = "meters";
y:axis = "Y";
y:valid_range = -9000000., 9000000.;
double x(x);
x:standard_name = "projection_x_coordinate" ;
x:coverage_content_type = "coordinate" ;
x:long_name = "x" ;
x:units = "meters";
x:axis = "X";
x:valid_range = -9000000., 9000000.;
char crs ;
crs:grid_mapping_name = "lambert_azimuthal_equal_area" ;
crs:longitude_of_projection_origin = 0. ;
crs:latitude_of_projection_origin = 90. ;
crs:false_easting = 0. ;
crs:false_northing = 0. ;
crs:semi_major_axis = 6378137. ;
crs:inverse_flattening = 298.257223563 ;
crs:proj4text = "+proj=laea +lat_0=90 +lon_0=0 +x_0=0 +y_0=0 +ellps=WGS84 +datum=WGS84 +
crs:srid = "urn:ogc:def:crs:EPSG::6931" ;
crs:coverage_content_type = "auxiliaryInformation" ;
crs:references = "[\"EASE-Grid 2.0 documentation: http://nsidc.org/data/ease/ease_grid2.
crs:crs_wkt = "PROJCRS[\"WGS 84 / NSIDC EASE-Grid 2.0 North\", BASEGEODCRS[\"WGS 84\", D
crs:long_name = "EASE2_N3.125km" ;
short SigmaO_ave(time, y, x);
SigmaO_ave:standard_name = "brightness_temperature" ;
SigmaO_ave:long_name = "SIR SigmaO";
Sigma0_ave:units = "1";
SigmaO_ave:_FillValue = -32768s;
SigmaO_ave:valid_range = 0s, 32767s;
Sigma0_ave:packing_convention = "netCDF" ;
SigmaO_ave:packing_convention_description = "unpacked = scale_factor*packed + add_offset
```

```
SigmaO_ave:scale_factor = 0.002f ;
SigmaO_ave:add_offset = -55.f ;
SigmaO_ave:grid_mapping = "crs";
Sigma0_ave:coverage_content_type = "image" ;
short SigmaO_slope_ave(time, y, x);
Sigma0_slope_ave:standard_name = "brightness_temperature" ;
SigmaO_slope_ave:long_name = "SIR SigmaO slope" ;
SigmaO_slope_ave:units = "1";
SigmaO_slope_ave:_FillValue = -32768s ;
Sigma0_slope_ave:valid_range = 0s, 32767s ;
SigmaO_slope_ave:packing_convention = "netCDF" ;
SigmaO_slope_ave:packing_convention_description = "unpacked = scale_factor*packed + add_
Sigma0_slope_ave:scale_factor = 0.001f ;
Sigma0_slope_ave:add_offset = -2.f ;
Sigma0_slope_ave:grid_mapping = "crs";
Sigma0_slope_ave:coverage_content_type = "image" ;
short SigmaO(time, y, x) ;
Sigma0:standard_name = "brightness_temperature" ;
Sigma0:long_name = "SIR Sigma0" ;
Sigma0:units = "1";
Sigma0:_FillValue = -32768s;
Sigma0:valid_range = 0s, 32767s;
Sigma0:packing_convention = "netCDF" ;
SigmaO:packing_convention_description = "unpacked = scale_factor*packed + add_offset";
Sigma0:scale_factor = 0.002f;
Sigma0:add_offset = -55.f;
Sigma0:grid_mapping = "crs";
Sigma0:coverage_content_type = "image";
Sigma0:sir_number_of_iterations = 30 ;
Sigma0:median_filter = 1 ;
Sigma0:temporal_division = "Both" ;
SigmaO:temporal_division_local_start_time = 5.f ;
Sigma0:temporal_division_local_end_time = 17.f ;
SigmaO:frequency_and_polarization = "14.6VV" ;
short SigmaO_slope(time, y, x);
Sigma0_slope:standard_name = "brightness_temperature" ;
SigmaO_slope:long_name = "SIR SigmaO slope" ;
SigmaO_slope:units = "1";
SigmaO_slope:_FillValue = -32768s;
SigmaO_slope:valid_range = 0s, 32767s;
```

```
Sigma0_slope:packing_convention = "netCDF" ;
SigmaO_slope:packing_convention_description = "unpacked = scale_factor*packed + add_offs
Sigma0_slope:scale_factor = 0.001f ;
SigmaO_slope:add_offset = -2.f ;
Sigma0_slope:grid_mapping = "crs";
Sigma0_slope:coverage_content_type = "image" ;
short SigmaO_num_samples(time, y, x);
SigmaO_num_samples:long_name = "SIR Number of Measurements" ;
SigmaO_num_samples:units = "count";
SigmaO_num_samples:_FillValue = Os ;
SigmaO_num_samples:valid_range = 1s, 255s ;
Sigma0_num_samples:grid_mapping = "crs" ;
SigmaO_num_samples:coverage_content_type = "auxiliaryInformation" ;
short Incidence_angle(time, y, x);
Incidence_angle:standard_name = "angle_of_incidence" ;
Incidence_angle:long_name = "SIR Incidence Angle" ;
Incidence_angle:units = "degree" ;
Incidence_angle:_FillValue = -1s ;
Incidence_angle:valid_range = 0s, 9000s ;
Incidence_angle:packing_convention = "netCDF" ;
Incidence_angle:packing_convention_description = "unpacked = scale_factor*packed + add_o
Incidence_angle:scale_factor = 0.01f ;
Incidence_angle:add_offset = 0.f ;
Incidence_angle:grid_mapping = "crs";
Incidence_angle:coverage_content_type = "auxiliaryInformation" ;
short Sigma0_std_dev(time, y, x);
SigmaO_std_dev:long_name = "SIR SigmaO standard deviation" ;
Sigma0_std_dev:units = "1";
SigmaO_std_dev:_FillValue = -32768s ;
SigmaO_std_dev:valid_range = -32766s, 32767s;
Sigma0_std_dev:packing_convention = "netCDF" ;
SigmaO_std_dev:packing_convention_description = "unpacked = scale_factor*packed + add_of
Sigma0_std_dev:scale_factor = 0.002f ;
SigmaO_std_dev:add_offset = 0.f ;
Sigma0_std_dev:grid_mapping = "crs" ;
Sigma0_std_dev:coverage_content_type = "auxiliaryInformation" ;
short SigmaO_time(time, y, x);
SigmaO_time:long_name = "Time of Day" ;
SigmaO_time:units = "minutes since 1978-09-27 00:00:00";
SigmaO_time:_FillValue = -32768s;
```

```
SigmaO_time:valid_range = -32767s, 32767s;
SigmaO_time:packing_convention = "netCDF" ;
SigmaO_time:packing_convention_description = "unpacked = scale_factor*packed + add_offse
SigmaO_time:scale_factor = 1.f ;
SigmaO_time:add_offset = 0.f ;
SigmaO_time:grid_mapping = "crs" ;
SigmaO_time:coverage_content_type = "auxiliaryInformation" ;
SigmaO_time:calendar = "gregorian" ;
// global attributes:
:references = "Early, D. S., and D.G. Long. 2001. Image Reconstruction and Enhanced Reso
:title = "SASS Radar Twice-Daily SIRF-Enhanced EASE-Grid 2.0 Sigma0";
:id = "doi:10.5067/46IY83E4HHJU";
:summary = "Enhanced-resolution, gridded SASS Ku-band radar backscatter";
:project = "Scatterometer Climate Record Pathfinder" ;
:contributor_name = "David G. Long, NASA Scatterometer Climate Record Pathfinder";
:contributor_role = "Principal Investigator and Developer, Data Producer" ;
:citation = "D. G. Long\nSASS Twice-Daily SIRF-Enhanced EASE-Grid 2.0 Sigma0.\nVersion 1
:license = "These data are freely, openly, and fully available to use without\nrestricti
:Conventions = "CF-1.6, ACDD-1.3";
:product_version = "v1.0";
:software_version_id = "1.0.0";
:software_repository = "" ;
:history = "sass_meta_sir_cetb" ;
:comment = "Epoch date for data in this file: 1978-09-27 00:00:00Z";
:source = "doi:TBD (SASS SDR): See input_fileN list and number_of_input_files attributes
:metadata_link = "http://www.scp.byu.edu/" ;
:institution = "Scatterometer Climate Record Pathfinder\nElectrical and Computer Enginee
:publisher_name = "Scatterometer Climate Record Pathfinder" ;
:publisher_type = "institution" ;
:publisher_url = "http://www.scp.byu.edu" ;
:publisher_email = "long@ee.byu.edu" ;
:program = "NASA Earth Science Data and Information System (ESDIS)";
:standard_name_vocabulary = "CF Standard Name Table (v27, 28 September 2013)";
:cdm_data_type = "Grid" ;
:keywords = "EARTH SCIENCE > SPECTRAL/ENGINEERING > MICROWAVE > RADAR BACKSCATTER" ;
:keywords_vocabulary = "NASA Global Change Master Directory (GCMD) Earth Science Keyword
:platform = "SASS > SASS Scatterometer on Seasat-A" ;
:platform_vocabulary = "NASA Global Change Master Directory (GCMD) Earth Science Keyword
:instrument = "SASS Ku-BAND RADAR > SASS Ku-Band Radar";
```

```
:instrument_vocabulary = "NASA Global Change Master Directory (GCMD) Earth Science Keywo
:time_coverage_resolution = "P1d";
:geospatial_bounds = "" ;
:geospatial_bounds_crs = "" ;
:geospatial_x_units = "meters" ;
:geospatial_y_units = "meters" ;
:naming_authority = "org.doi.dx" ;
:date_created = "2023-01-05T00:25:04GMT" ;
:date_modified = "2023-01-05T00:25:04GMT";
:date_issued = "2023-01-05T00:25:04GMT";
:date_metadata_modified = "2023-01-05T00:25:04GMT" ;
:input_data_quality_filtering = "Only used highest-quality input data." ;
:acknowledgement = "This data set was created with funding from NASA Grant #TBD.";
:processing_level = "Level 3";
:creator_name = "David Long" ;
:creator_type = "person" ;
:creator_email = "long@ee.byu.edu" ;
:creator_url = "http://www.scp.byu.edu" ;
:creator_institution = "Electrical and Computer Engineering Department\nBrigham Young Un
:geospatial_lat_min = 0. ;
:geospatial_lat_max = 90. ;
:geospatial_lon_min = -180.;
:geospatial_lon_max = 180.;
:geospatial_lat_units = "degrees_north" ;
:geospatial_lon_units = "degrees_east" ;
:geospatial_x_resolution = "3125.00 meters" ;
:geospatial_y_resolution = "3125.00 meters" ;
:time_coverage_start = "1978-09-04T07:11:00.00Z";
:time_coverage_end = "1978-10-19T17:01:00.00Z";
:time_coverage_duration = "P45T09:50:00.00";
:number_of_input_files = 42;
:input_file1 = "sass-269-1.sb";
:input_file2 = "sass-269-2.sb";
:input_file3 = "sass-269-3.sb";
:input_file4 = "sass-269-4.sb"
:input_file5 = "sass-270-1.sb" ;
:input_file6 = "sass-270-2.sb";
:input_file7 = "sass-270-4.sb";
:input_file8 = "sass-270-5.sb";
:input_file9 = "sass-271-1.sb";
```

```
:input_file10 = "sass-271-2.sb";
:input_file11 = "sass-271-3.sb";
:input_file12 = "sass-271-5.sb"
:input_file13 = "sass-272-1.sb" ;
:input_file14 = "sass-272-2.sb"
:input_file15 = "sass-272-3.sb"
:input_file16 = "sass-272-4.sb"
:input_file17 = "sass-272-5.sb"
:input_file18 = "sass-273-1.sb"
:input_file19 = "sass-273-2.sb"
:input_file20 = "sass-273-3.sb"
:input_file21 = "sass-273-4.sb"
:input_file22 = "sass-274-1.sb"
:input_file23 = "sass-274-2.sb"
:input_file24 = "sass-274-3.sb" ;
:input_file25 = "sass-274-4.sb"
:input_file26 = "sass-275-1.sb"
:input_file27 = "sass-275-2.sb"
:input_file28 = "sass-275-3.sb"
:input_file29 = "sass-275-4.sb"
:input_file30 = "sass-276-1.sb"
:input_file31 = "sass-276-2.sb"
:input_file32 = "sass-276-3.sb"
:input_file33 = "sass-276-4.sb"
:input_file34 = "sass-277-1.sb"
:input_file35 = "sass-277-2.sb"
:input_file36 = "sass-277-3.sb"
:input_file37 = "sass-277-4.sb"
:input_file38 = "sass-278-1.sb"
:input_file39 = "sass-278-2.sb"
:input_file40 = "sass-278-3.sb";
:input_file41 = "sass-278-4.sb";
:input_file42 = "sass-278-5.sb";
}
```